The core of a complex manifold

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The core $\mathfrak{c}(\mathcal{M})$ of a complex manifold $\mathcal{M}$ is introduced as the set of all points where every smooth and bounded from above plurisubharmonic function on $\mathcal{M}$ fails to be strictly plurisubharmonic.

I will explain that every strictly pseudoconvex domain $\Omega \subset \mathcal{M}$ with smooth boundary admits a global defining function that is strictly plurisubharmonic precisely in the complement of $\mathfrak{c}(\Omega)$. Moreover, I will discuss properties of the core, in particular

1. 1-pseudoconcavity of the core, and
2. Liouville type properties of the core.