On Lane-Emden type Equations of Higher Order

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In this talk, we discuss a Lane-Emden type equation of higher order with a supercritical polynomial non-linearity

$$(-1)^m \Delta^m u = |u|^{p-2} u$$

 $m\in\mathbb{N}$ with n>2m and $p>p^*=\frac{2n}{n-2m}.$ For m=1 this equation was proposed by Lane to study the interior of a star.

We will discuss some new and well-known results for these equations. In the center of our attention will be a new monotonicity formula for the triharmonic case m=3 for certain combinations of p and n. This formula will allow us to bound the Hausdorff-dimension of the singular set of stationary solutions.